



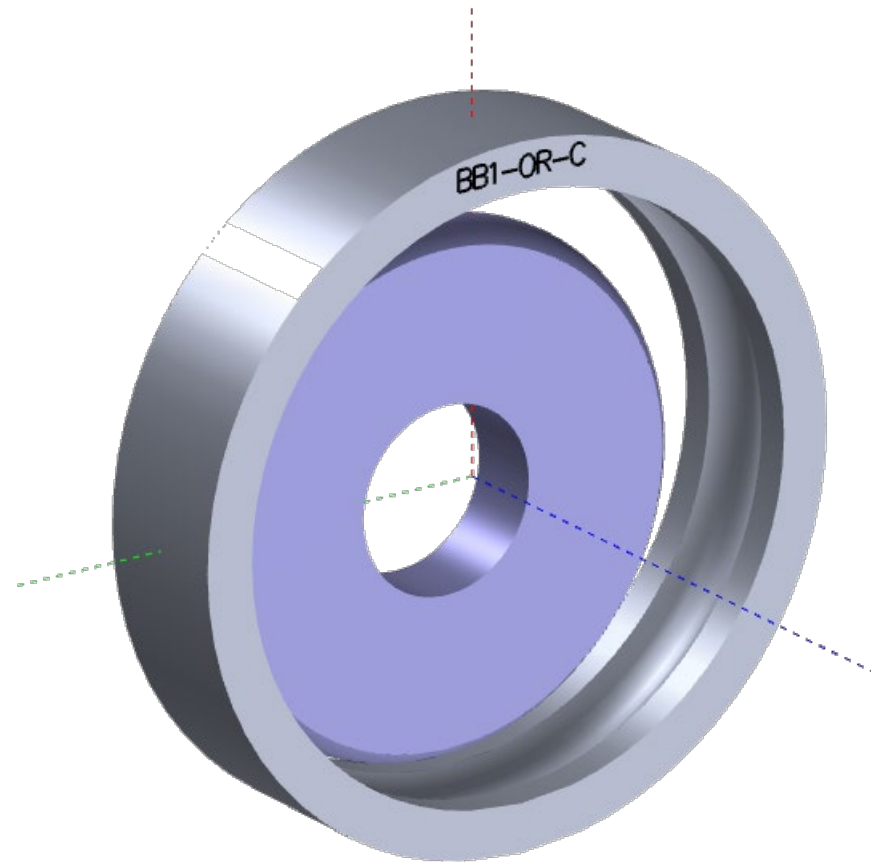
# TLM, FMI & EXTRIPOL: Acronyms for Stable Co-simulation?

Robert Braun

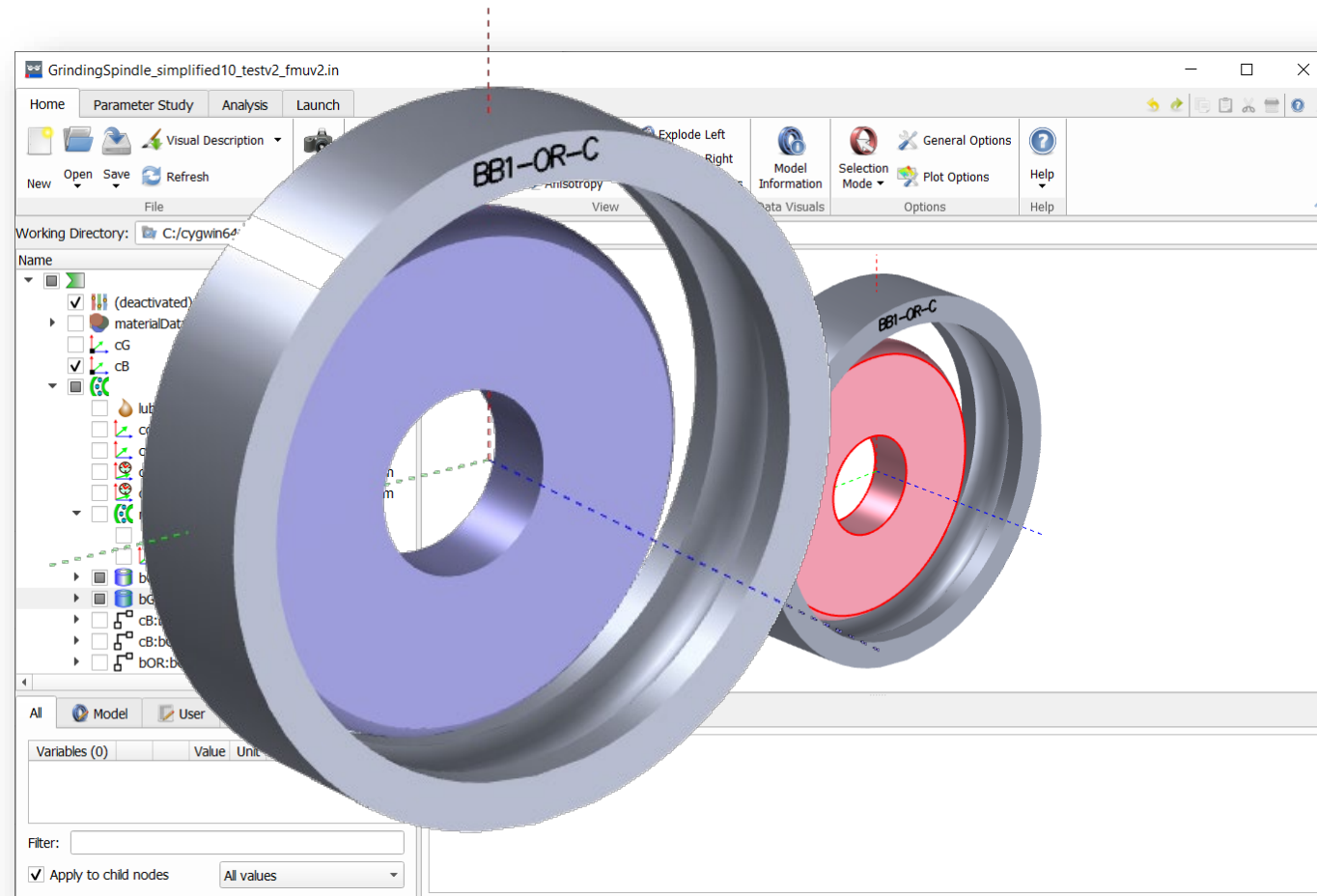
# Acronyms?

- FMI – Functional Mockup Interface
- TLM – Transmission Line Modelling
- EXTRIPOL – Extrapolated Interpolation
- BEAST – Beating Simulation Tool

# Grinding Co-simulation



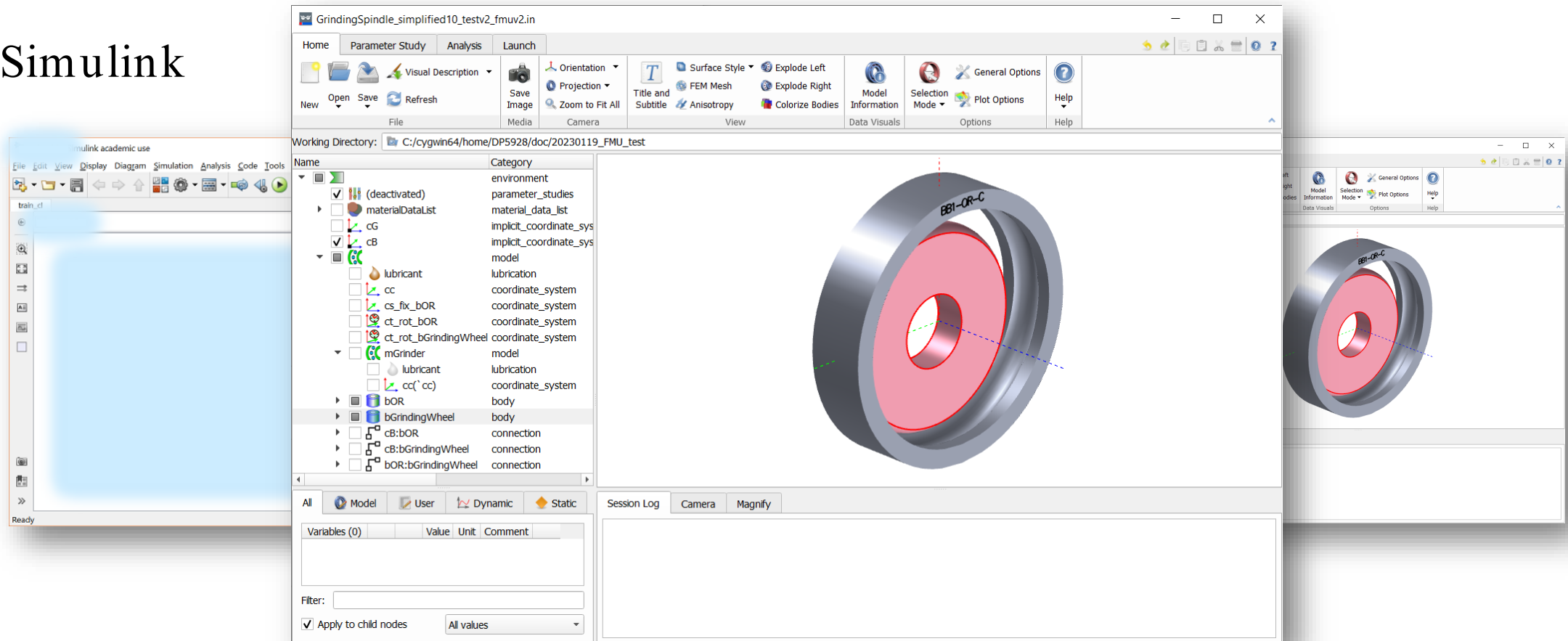
# BEAST – BEARing Simulation Tool



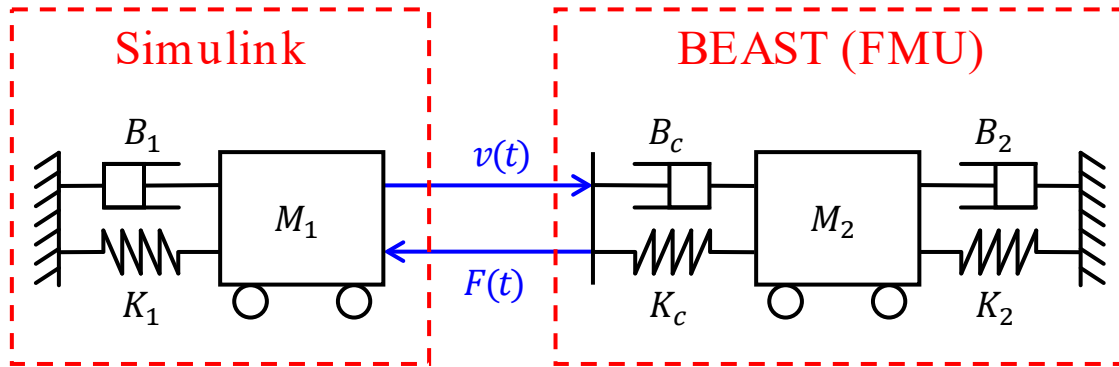


# Functional Mockup Interface

Simulink

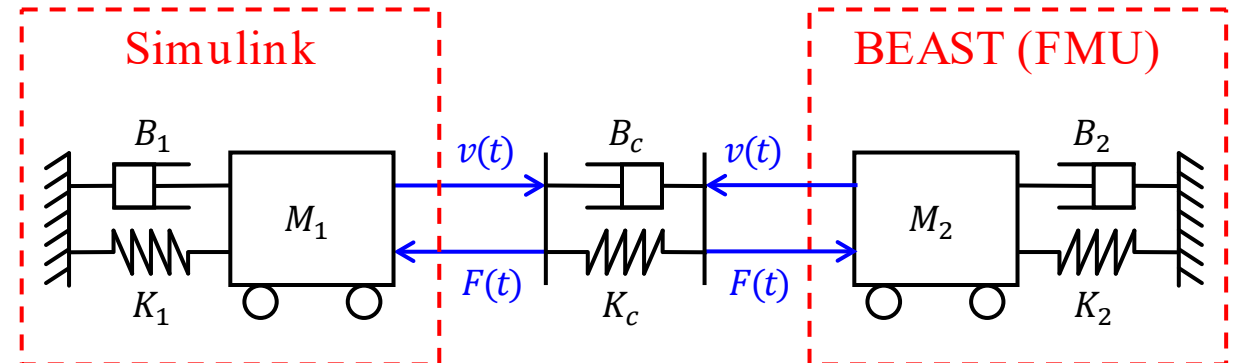


# Approaches

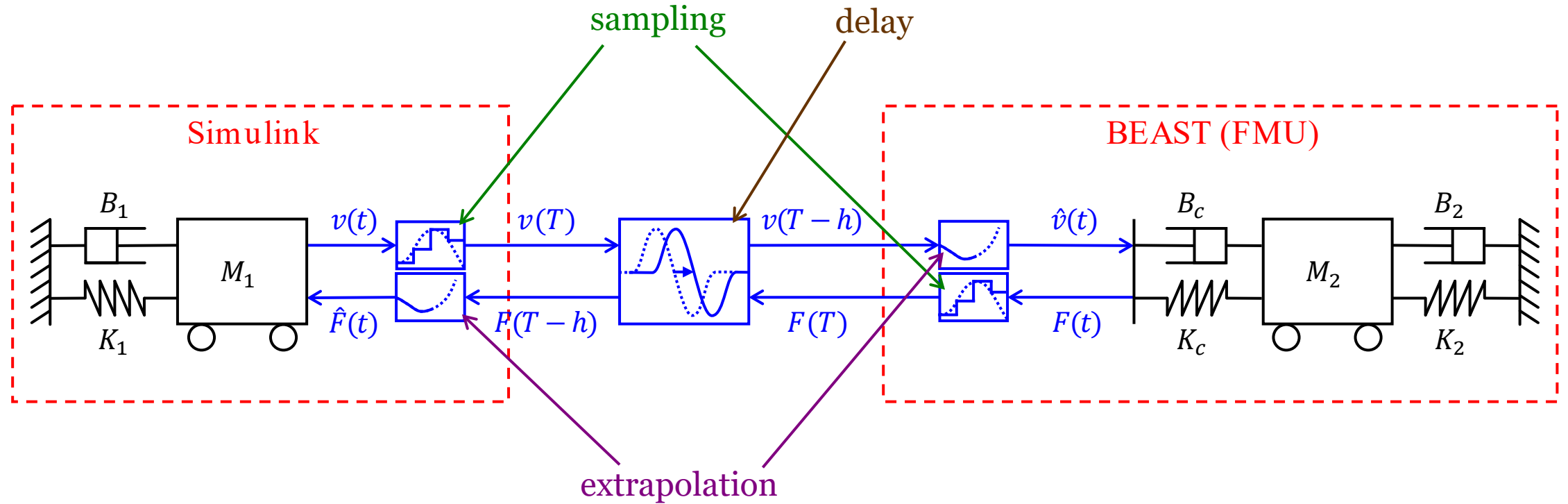


Force-displacement coupling

Force-force coupling  
(using TLM)

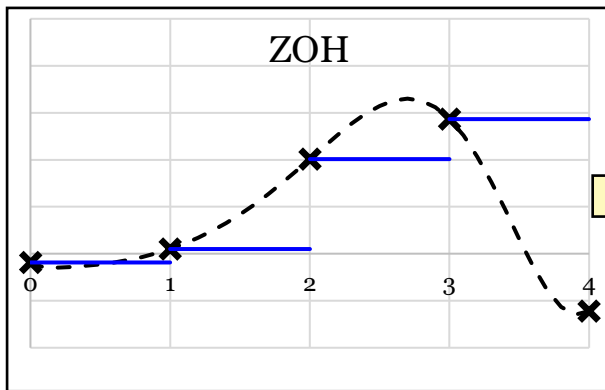


# Force-Displacement Coupling

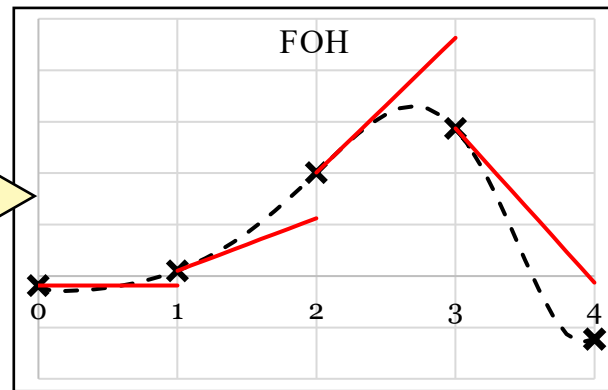


# Extrapolation

Before project:  
Zero-order hold



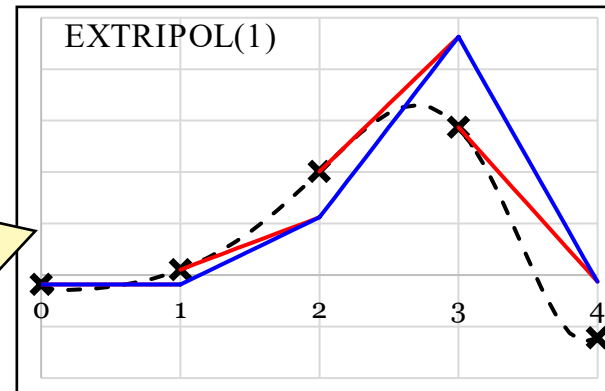
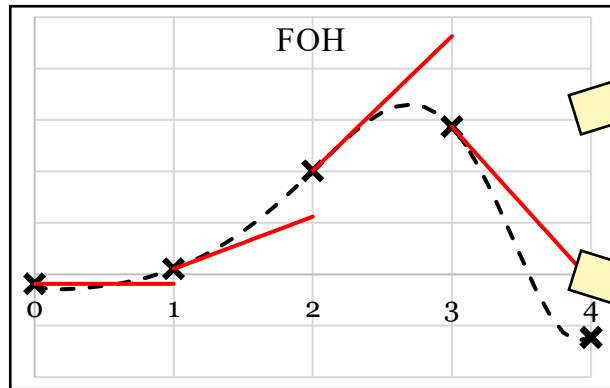
First improvement:  
First-order hold



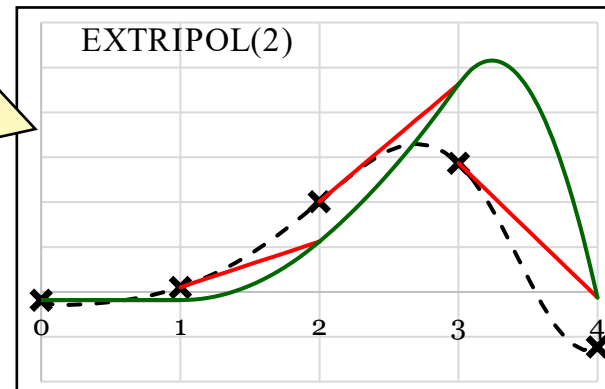
Problem : Input still discontinuous  $\Rightarrow$  solver restarts



# Extrapolated Interpolation (EXTRIPOL)

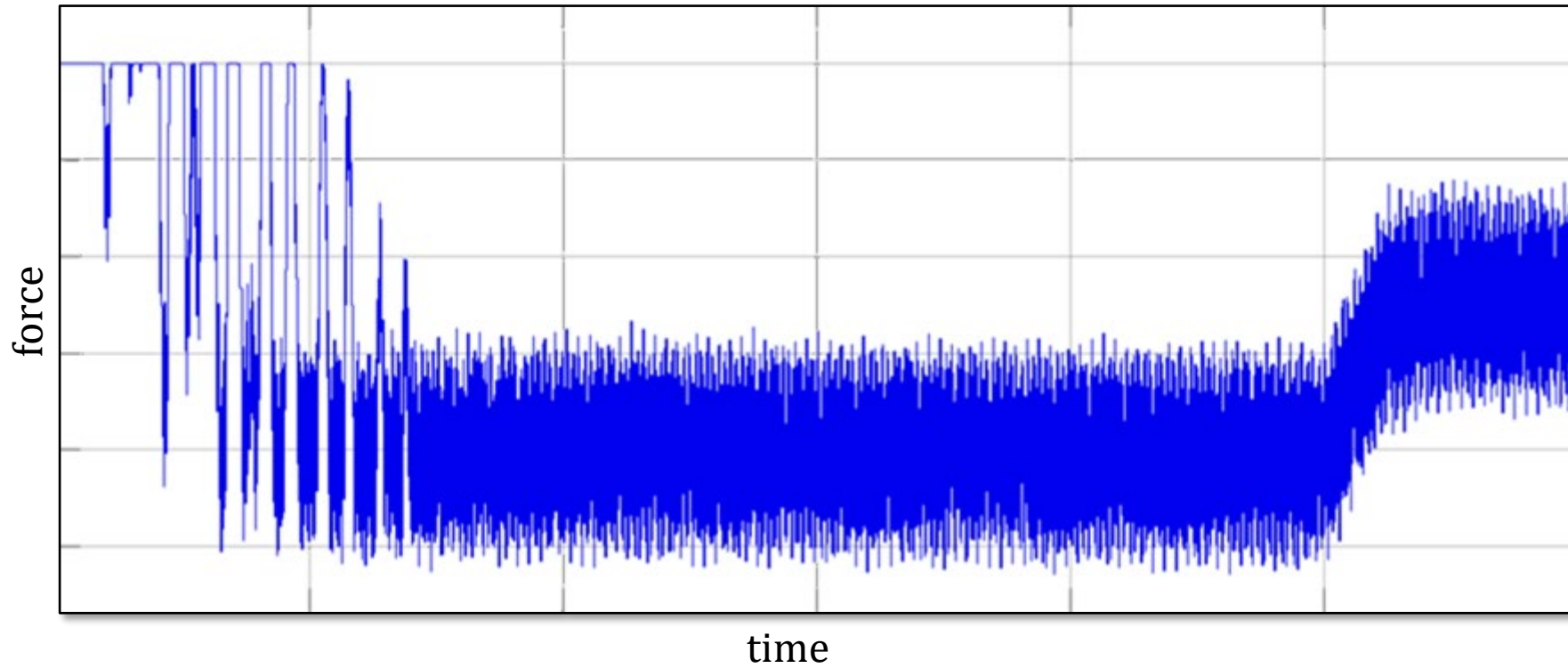


$C^0$  continuity



$C^1$  continuity

# Co-Simulation Results

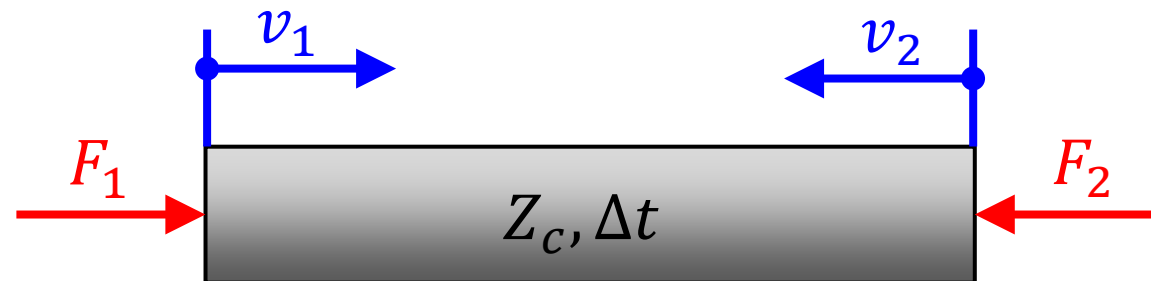


# What about stability?



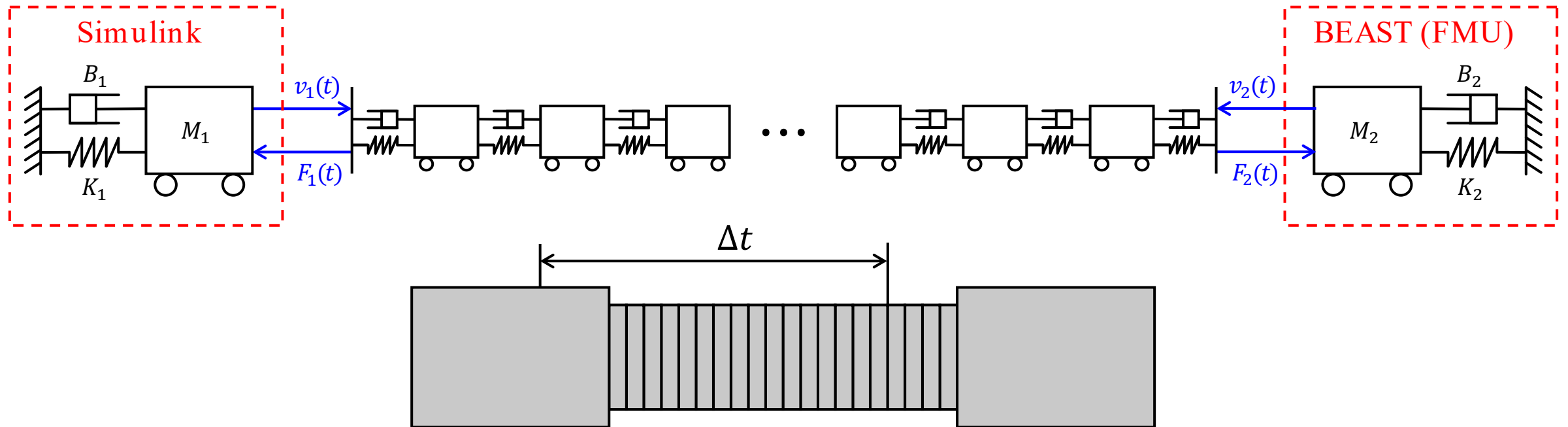
# Transmission Line Modelling

- Extrapolation seems to work, but cannot guarantee stability
- Artificial time delay between velocity and force
- Potential solution: TLM?



# Transmission Line Modelling (TLM)

Imagine force-force coupling with distributed inertia:



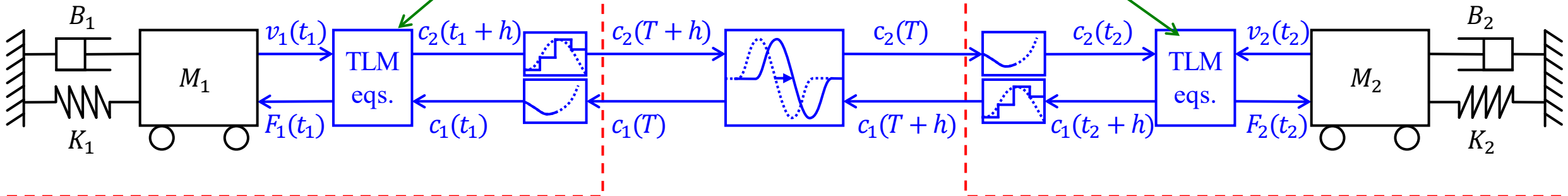
Enables communication delay without numerical instability!

# TLM with FMI 1.0 and 2.0

TLM boundary equations

Simulink

BEAST (FMU)



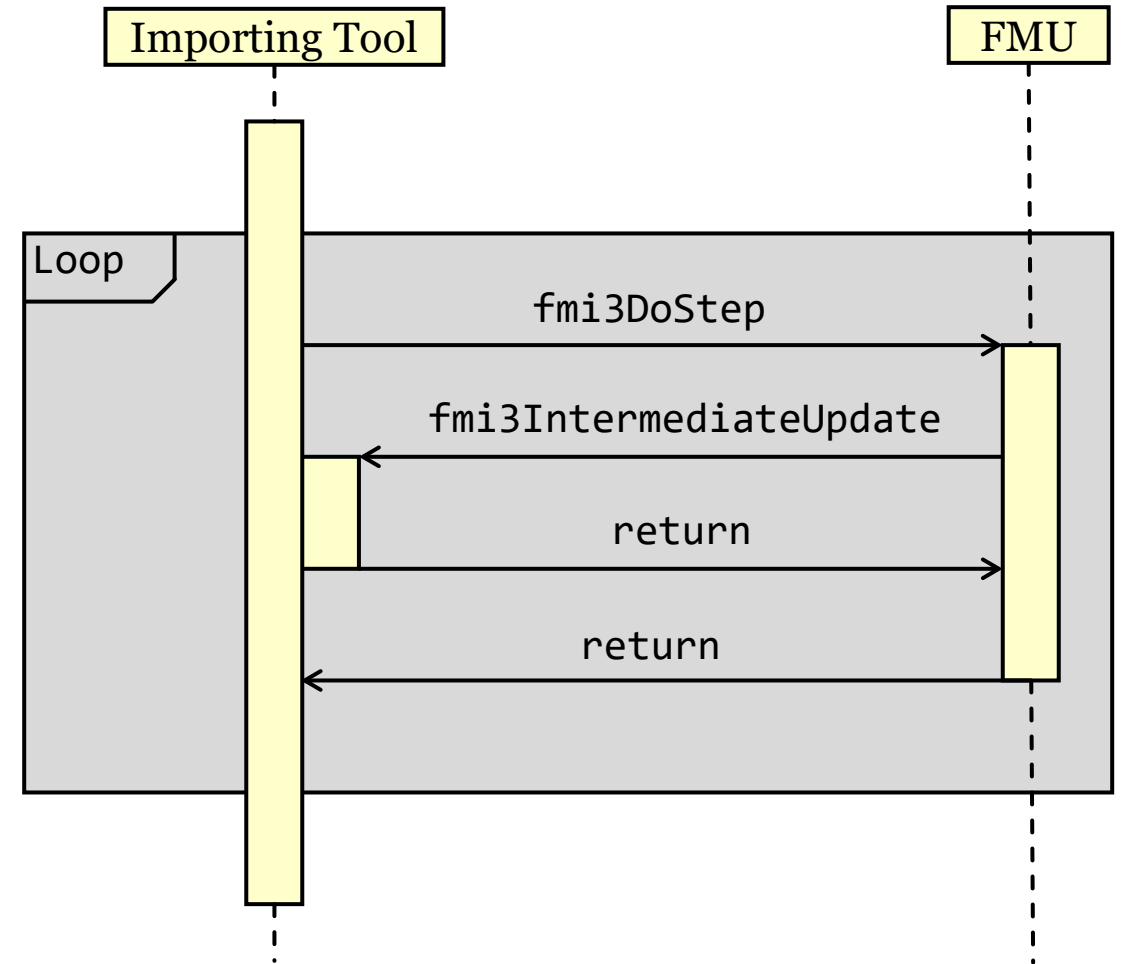
$$F_1(t) = c_1(t) + v_1(t)Z_c(t)$$

$$F_2(t) = c_2(t) + v_2(t)Z_c(t)$$

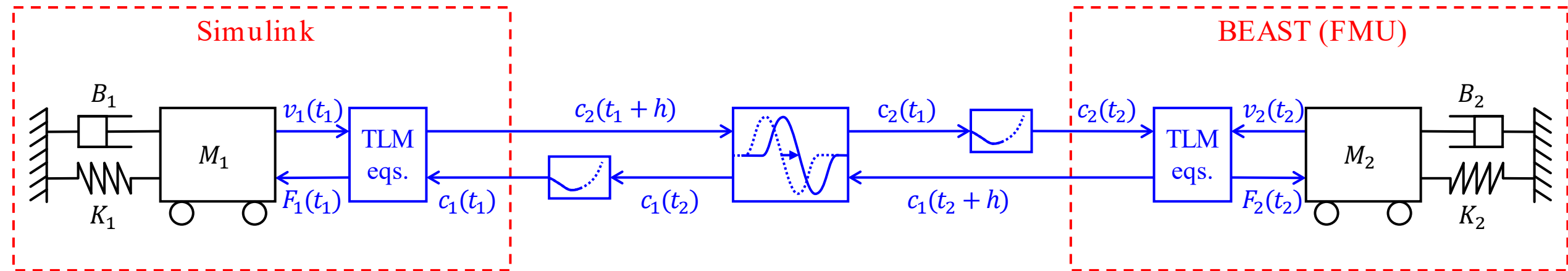


# TLM with FMI 3.0

- Change proposal submitted during ITEA3 OpenCPS project
- FMUs can request and provide intermediate variables
- Released in 2022



# TLM with FMI 3.0



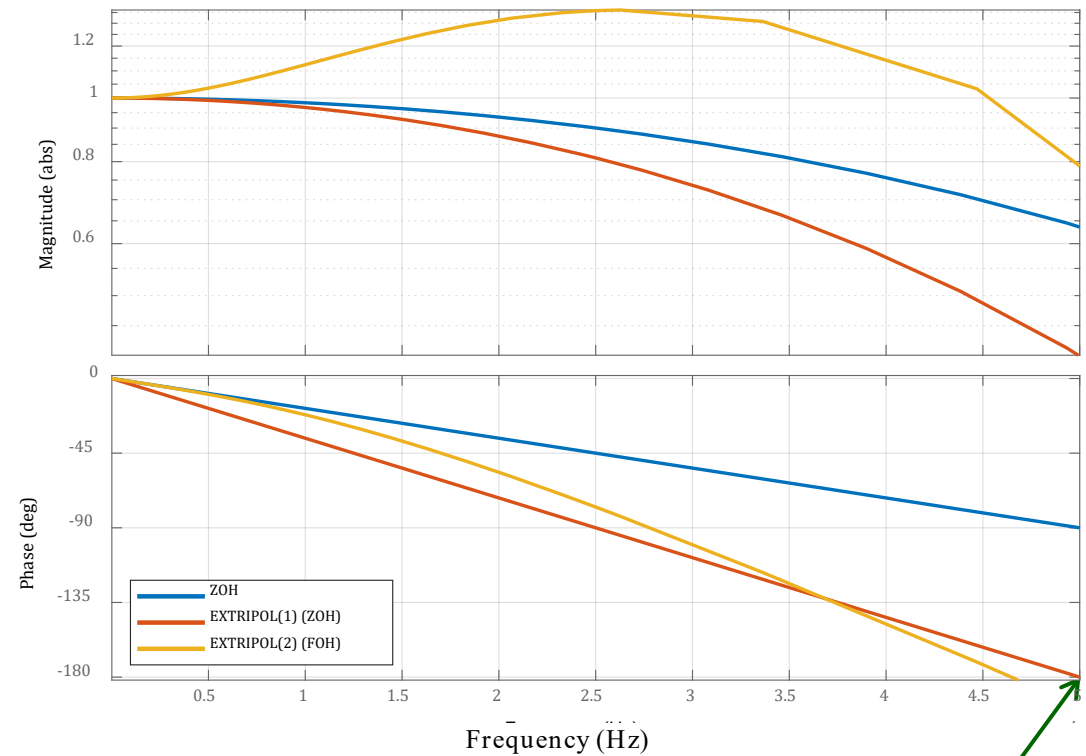
- Requires dedicated master simulation tool
- FMI 3.0 not (yet) supported by Simulink

# Frequency Domain Analysis

Potential problem:

- Reduced phase stability
- Energy balance affected


Bode diagram



Nyquist frequency

# Conclusions and Outlook

- EXTRIPOL
  - Recreates continuous data from sampled inputs
  - Fewer solver restarts
- TLM
  - Provides numerical stability
- FMI3
  - TLM co-simulation with continuous data exchange
  - Requires dedicated master simulation tool
  - Not yet supported by most tools
- FMI2 and TLM can be used together with EXTRIPOL



Thank you for listening!

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