

# Time Effective Testing and Compact Modeling of Electrochemical Impedance Spectroscopy (EIS) for Lithium Ion Batteries

Rapid, Reliable, and Repeatable, EIS (R<sup>3</sup>EIS),

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# Ignition for the research and development

## Motivating Question from Industrial partner

- We build high quality battery packs but they are expensive
- High quality cells are needed for high quality packs and they are expensive
- We want to change supplier and ensure that the cells and packs are of high quality
- How can we quickly and non destructively test and qualify cells suppliers?
- Can we sort cells based on quality to build better packs?

## Requirement Specification – Desirable properties of the tester

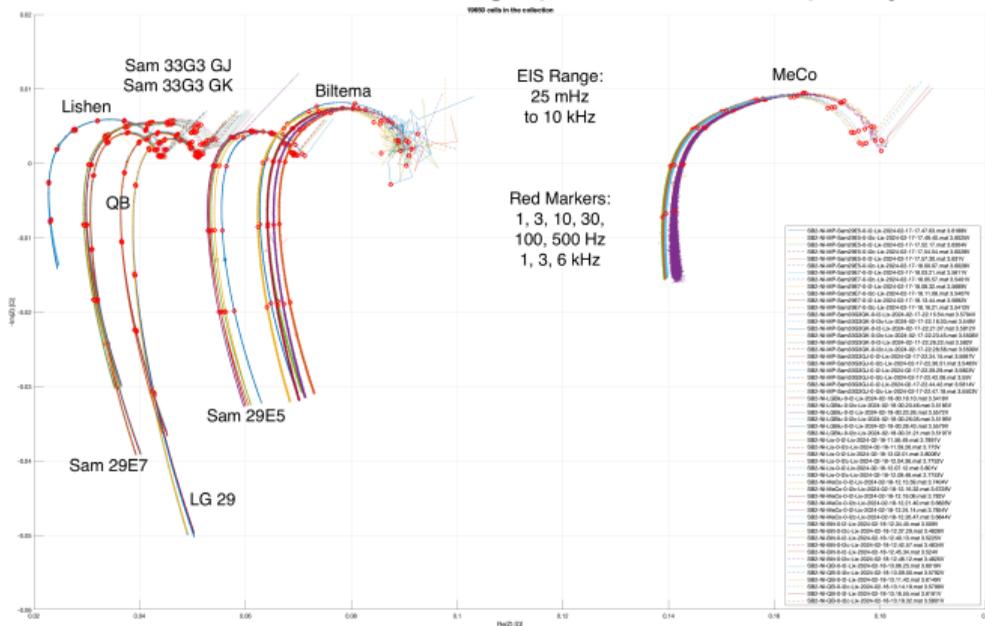
- Fast – Production line compatibility
- Non destructive – with high information content
- Repeatable – same result every time
- Cost effective – low cost per test

# Fundamental question: What is the **quality/properties/status** of a cell?

Battery resistance (impedance) → Some hints

Electrochemical Impedance Spectroscopy (EIS)

EIS → More detailed fingerprint  of cell quality.



- 1 What is EIS,  and Why is it Interesting?  
EIS - Examples of Connections to Battery State
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The Starting Point  
Signal design
- 3 Analysis tools – Extracting the ECM from the data
- 4 Questions and Discussion

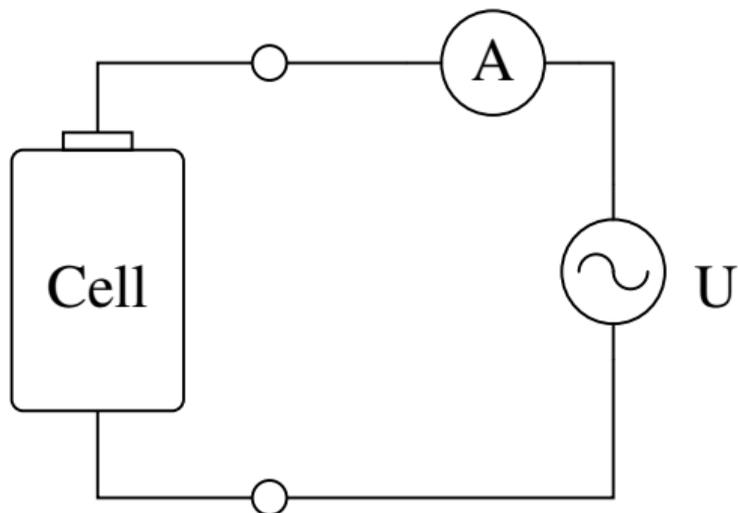
## Spectroscopy - Determine response

Measure  $U(\omega)$  and  $I(\omega)$  and calculate  $Z(\omega) = \frac{U(\omega)}{I(\omega)}$

Keep track of amplitude and phase - as complex number  $Z(\omega)$ .

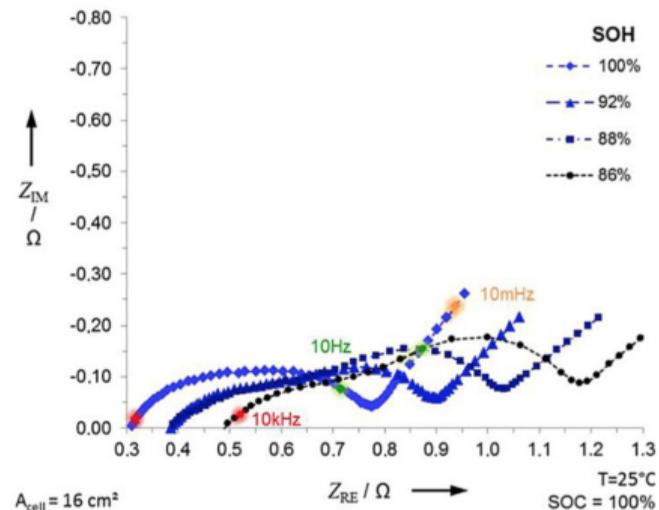
Plot the complex impedance  $Z(\omega)$ , with **negative imaginary axis**

- Nyquist plots



Impedance plot from Westerhoff et al. (2016).

Note arc/circle shapes



The Fingerprint, 

# Interpreting the – Equivalent Circuit Models (ECM)

## Ohms Law, Resistance, R

$$U = R \cdot I$$

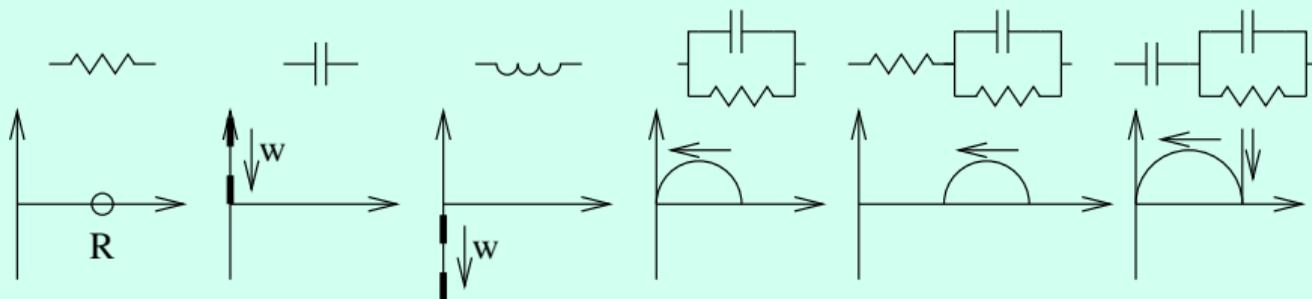
## Asymptotic properties and frequencies

	R	C	L
short circuit	0	$\omega \rightarrow \infty$	$\omega \rightarrow 0$
open circuit	$\infty$	$\omega \rightarrow 0$	$\omega \rightarrow \infty$

## Complex Impedance, Z

$$U = Z \cdot I$$

- Resistance  $Z_R = R$
- Capacitor  $Z_C = \frac{1}{j\omega C}$
- Inductor  $Z_L = j\omega L$



# Causes for impedances in a battery cell

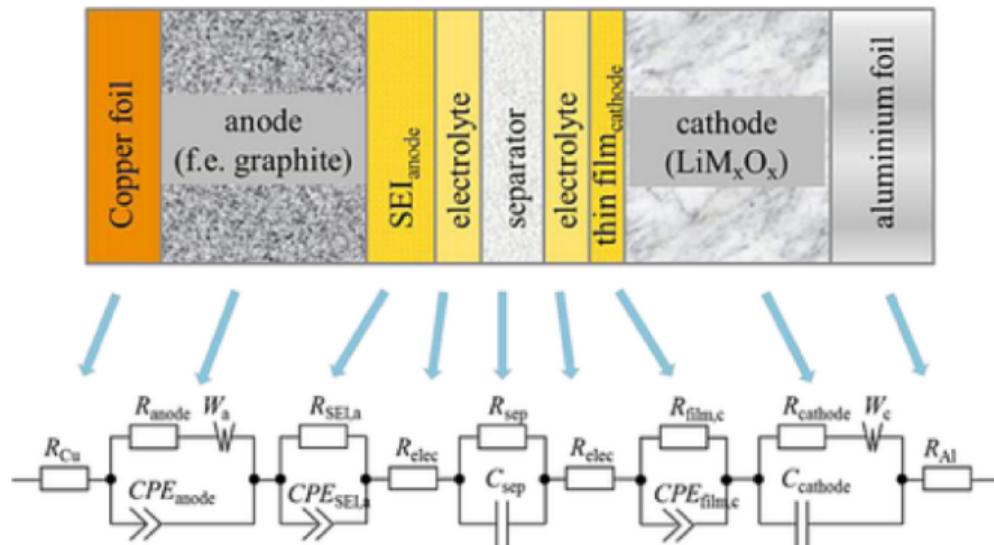


Figure from Westerhoff et al. (2016).

Material properties and physical processes like diffusion.

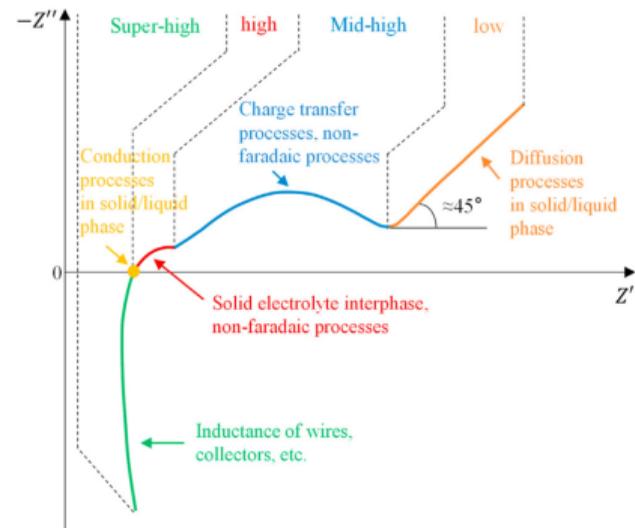


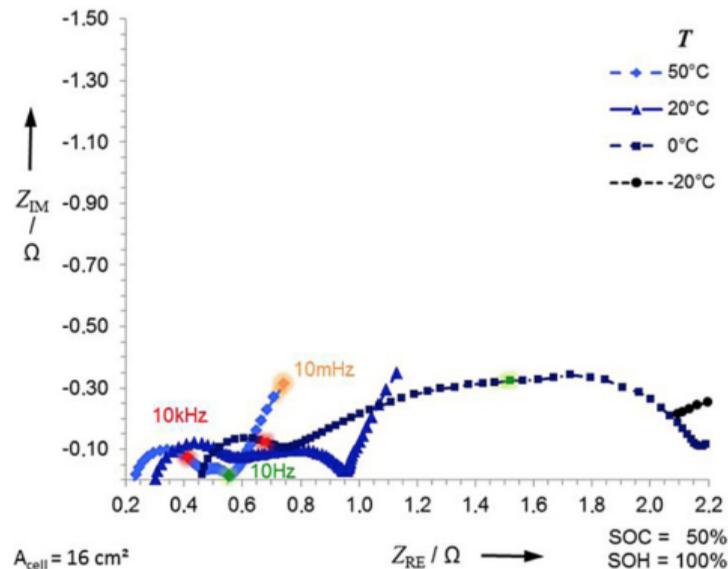
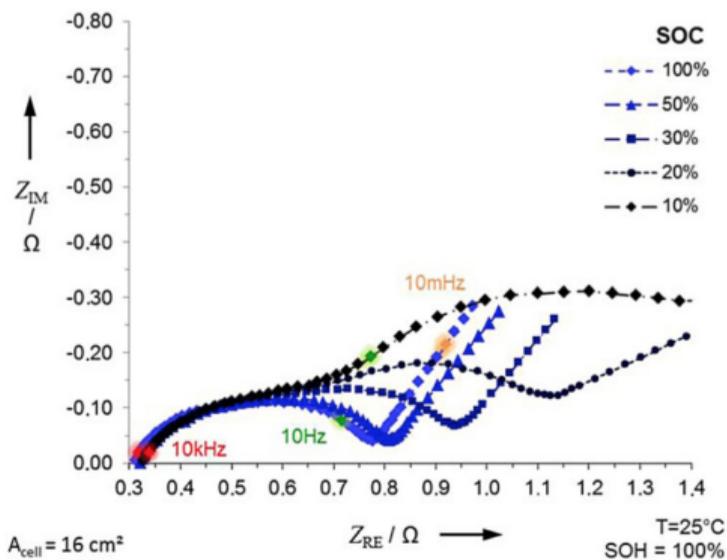
Figure from Wang et al. (2021)

# Why is EIS interesting?

## The impedance is rich in information

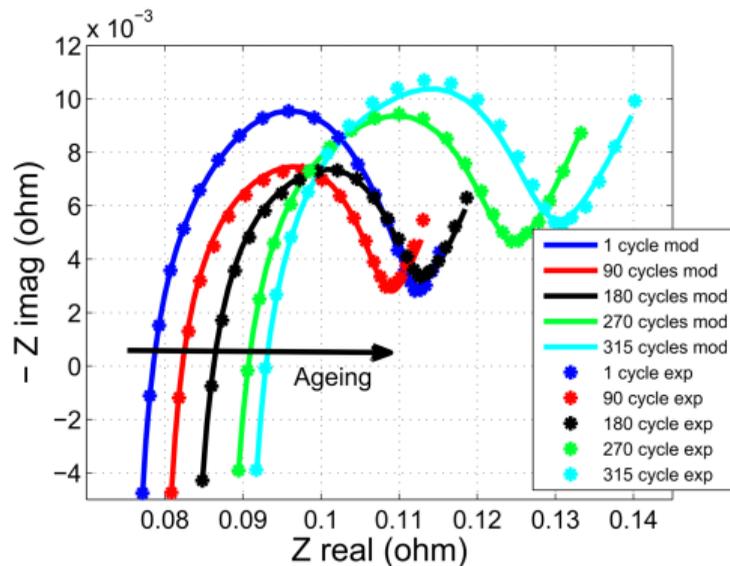
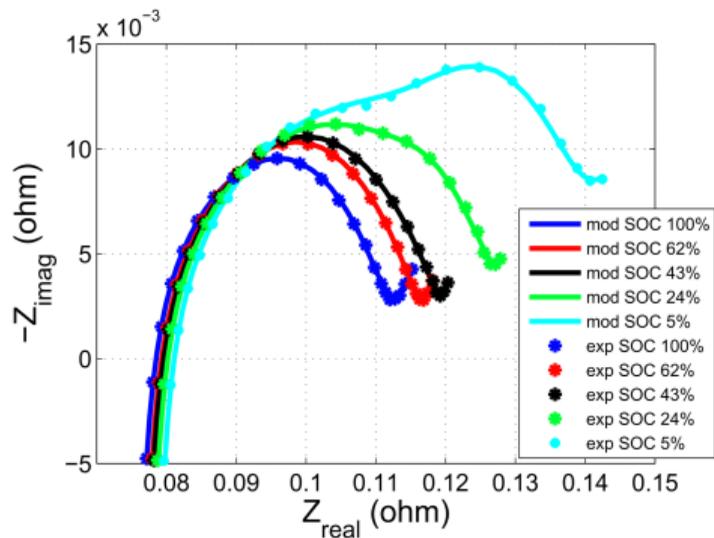
- More detailed information than resistance measurements.
  - Get a detailed fingerprint of the internal properties
- Non invasive test that exposes internal cell properties
  - State of charge – SOC
  - Temperature
  - State of health – SOH
  - Solid Electrolyte Interphase Size
  - Diagnostics
    - Internal Short - Dendrite connections
    - Thermal Runaway
    - Overcharge/Overdischarge
  - Production variations
- There is a vast knowledge base
- EIS, SOH and Battery search – More than 300 Scientific publications

# Spectroscopy – Shape depends on battery conditions SOC Temperature



Impedance plots from Westerhoff et al. (2016)

# Nyquist Diagram - Varying SoC and SoH

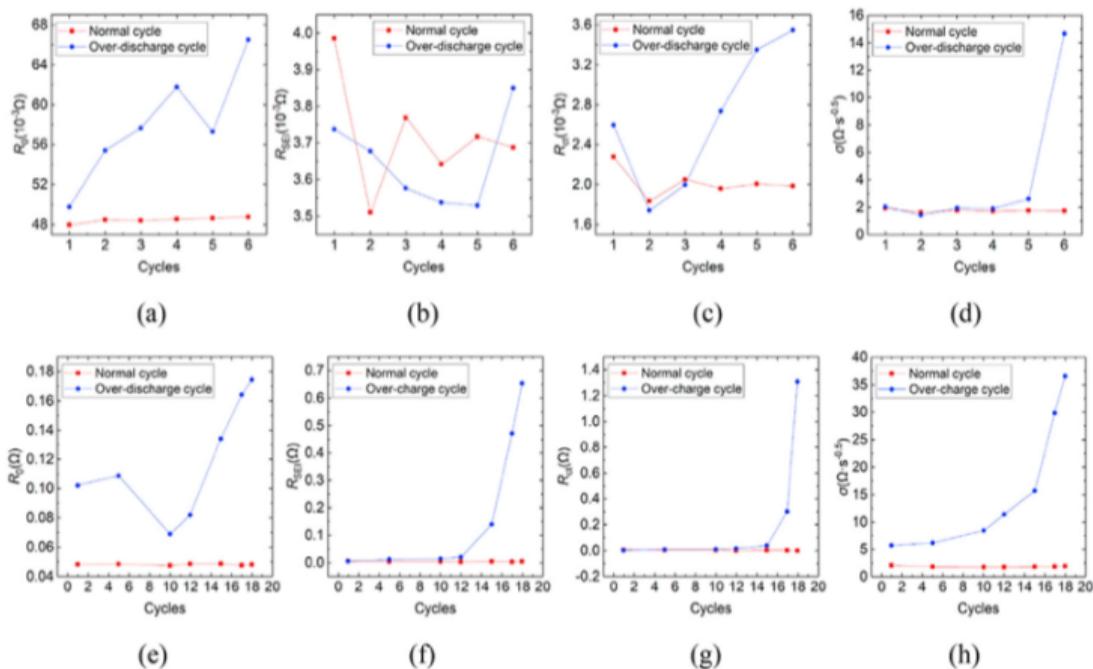


Impedance plots from Galeotti et al. (2015).

Much information in the fingerprint.

Shows that it is possible to decouple different internal properties effects.

# Over rated charging and discharging



**Fig. 19.** Changes of (a) (e) ohmic resistance  $R_0$ , (b) (f) SEI film resistance  $R_{SEI}$ , (c) (g) charge transfer resistance  $R_{ct}$ , and (d) (h) Warburg coefficient  $\sigma$  when the battery is over-discharged/charged.

Equivalent circuit parameters from Wang et al. (2021).

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# The Challenges and Path to a Solution

## My Spark ⚡ – The Challenge of Alelion

- Would like to buy cheaper cells.
- Ensure production of high quality batteries.

## General Challenges for Battery Quality

- The weakest link in a chain limits the chain strength.
  - Extends to batteries too
  - The weakest cell will limit the battery.
  - The weakest cell will be more stressed in use.
  - A weak cell degrades faster than the rest of the pack.
- Ensure all cells in a pack have equal performance.
  - Eliminate weak links.
  - Select cells that have equal or similar properties.
  - Equalizes aging of cells.

## Towards a Solution

- Need a powerful tool for quality assessment of cells
- Electrochemical Impedance Spectroscopy (EIS)
  - A lot of information about a cell in the result.
  - Give input stimuli and measure response.
  - Normal test with stimuli, **timeconsuming**.
- In an assembly line: short time-slots for measurements.
  - Challenge to extract information.
  - Solution: multi-spectral input signal.

# Basic differences – Traditional EIS and R<sup>3</sup>EIS Principle

## Traditional EIS – Used by PhDs

- Equilibrate the cell before measurement
- One single frequency at a time
- Measure steady state response
- Small signal amplitude
- Frequency sweep over the desired range
- Time consuming
- Battery can drift during measurement

## R<sup>3</sup>EIS Principle

- No equilibration – In operando
- Multiple frequencies simultaneously
- Measure transient response
- Sum of signal amplitude
- Designed multi-sine signal
- Fast measurement
- Snapshot of battery state

## Signal design for maximum information in minimum time

Many frequencies simultaneously – Limited Amplitude – Compile a smart signal

Not trivial – Requires expertise in signal processing and battery EIS

Many possible designs – Trade-off between time, resolution and accuracy

# The goal and challenges for an EIS tester implementation

## Challenge and limits

- **Goal:** How can we extract as much information as possible in a given time?
- What are the limits?
- Testing time sets the limit, on the lowest frequency. (Physics)  
 $f_{min} = \frac{1}{T}$  Hz, where  $T$  is the test time.
- Data Acquisition (DAQ) sets the limit on the highest frequency. (Nyquist theorem)  
 $f_{max} = \frac{f_s}{2}$  Hz, where  $f_s$  is the sampling frequency.
- Practical implementations have to obey these limits.
- Improvements in quality are possible by not going to the limits.

## Limits in current implementation – The frequency box

- $f_{min} = \frac{3}{T}$  Hz, there is an initial transient. (T is tuneable.)
- $f_{max} = \frac{f_s}{2 \cdot 20}$  Hz, 20 times over-sampling (10 kHz, but can go to 50 kHz).

# Signal design – Implementation

## Frequency selection

- Base frequency:  $f_0 = \frac{1}{T}$
- First used frequency:  $f_1 = k_1 f_0$ ,  $k_1 = 3$
- Avoid spread spectrum by separating frequencies

$$k_{n+1} \geq k_n + 10$$

except first 3 (use 3,7,13)

- Avoid harmonics by using  $k_n$  prime numbers

## Amplitude selection

- Define amplitude levels for each frequency, decay
- Ensure total amplitude stays within limits

## Theoretical limits

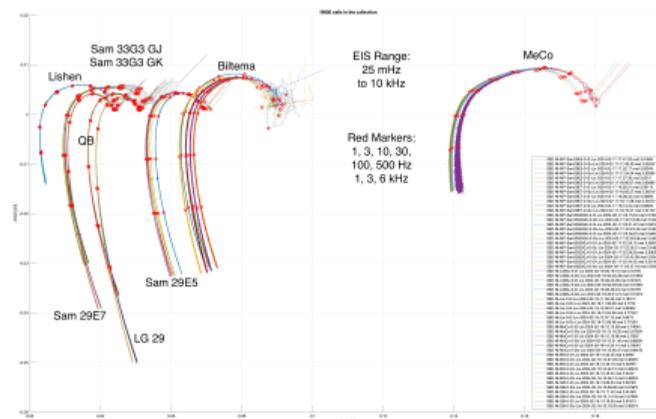
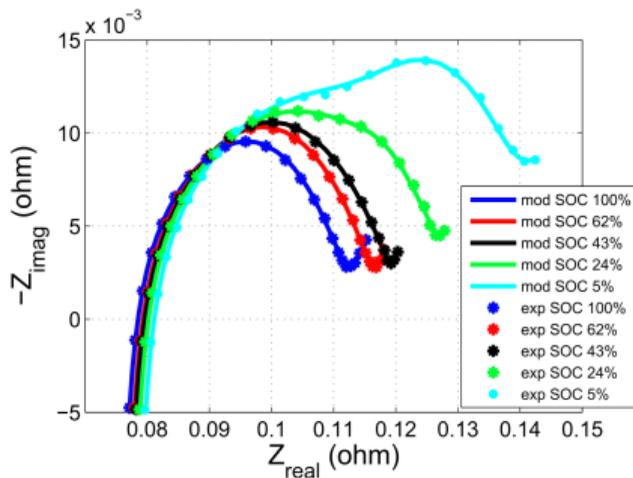
10 kHz @ 2 min → 60131 frequencies  
50 kHz @ 5 min → 670000 frequencies  
Extreme number of frequencies  
signal-to-noise ratio not optimal

## Introduce logspace (600 freq)

- Use logarithmic spacing for frequency selection
- Reduces the number of frequencies while maintaining coverage
- Improves signal-to-noise ratio

Low frequencies as dense as theory allows, high frequencies more sparse.

# Nyquist Diagrams – Traditional EIS and R<sup>3</sup>EIS Prototype



Traditional EIS 60 frequencies, 20 minutes.

R<sup>3</sup>EIS Prototype, 60131 frequencies, 2 minutes.

10 000 more data points per time units.

Users impressed by the resolution, repeatability and quality of the EIS results.

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# First Steps Towards Analysis of EIS Data with ECM

## Compact frequency domain modeling of equivalent circuits in Matlab

- Using anonymous functions in Matlab to define components
- Define rules for combining components in series and parallel

```
1 %%           Definitions of components and connections.
2 cap = @(C,w) 1./(i*w.*C);
3 res = @(R,w) R;
4 ind = @(L,w) L.*i.*w;
5 cpe = @(a,C,w) 1./((i*w).^a.*C);
6 cpeL= @(a,L,w) L.*(i*w).^a;
7 par = @(x,y) 1./(1./x+1./y);
8 ser = @(x,y) x + y;
9 ser3= @(x,y,z) x+y+z;
```

# Building System Models

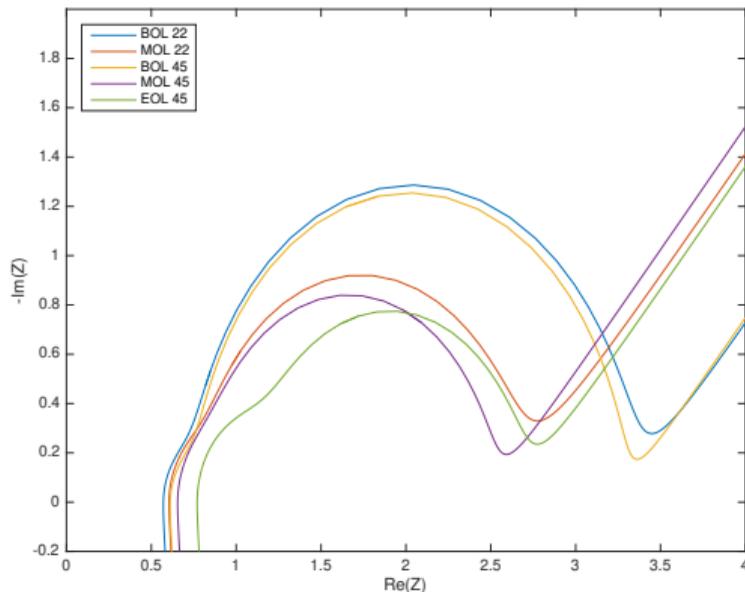
```
1 % Impedance models for Batteries from Literature
2 threeComp = @(p,w) ser(res(p.R_O,w) ,...
3                       par(cap(p.C_SEI,w) ,...
4                           res(p.R_CT,w)));
5 fiveComp   = @(p,w) ser(res(p.R_O,w) ,...
6                       par(cap(p.C_SEI,w) ,...
7                           ser(res(p.R_SEI,w) ,...
8                               par(cap(p.C_DL,w) , res(p.R_CT,w))))) );
9 sixComp    = @(p,w) ser(res(p.R_O,w) ,...
10                      par(cap(p.C_SEI,w) ,...
11                          ser(res(p.R_SEI,w) ,...
12                              par(cap(p.C_DL,w) ,...
13                                  ser(res(p.R_CT,w) , cap(p.C_W,w))))) );
14 % adding inductance and constant phase elements
15 sevenComp = @(p,w) ser3(cpeL(.95,1e-7,w) , res(p.R_O,w) ,...
16                        par(cap(p.C_SEI,w) ,...
17                            ser(res(p.R_SEI,w) ,...
18                                par(cap(p.C_DL,w) ,...
19                                    ser(res(p.R_CT,w) , cpe(.5 , p.C_W,w))))) );
```

# Generating EIS Cell Signatures - Frequency

```

1 EOL45_0.R_CT=1.18e-3;
2 EOL45_0.R_SEI=.70e-3;
3 EOL45_0.C_DL=214.5;
4 EOL45_0.C_SEI=50.1;
5 EOL45_0.C_W=12.20e3;
6
7 %%           Define Frequency Range
8 omega=logspace(-3,5,100);
9
10 %%          Do some plots
11 figure(1); clf
12 plot(sixComp(BOL22_0,omega) '*1e3')
13 hold on
14 plot(sixComp(MOL22_0,omega) '*1e3')
15 plot(sixComp(BOL45_0,omega) '*1e3')
16 plot(sixComp(MOL45_0,omega) '*1e3')
17 plot(sixComp(EOL45_0,omega) '*1e3')
18 axis([0 4 -.2 2])
19 legend('BOL 22','MOL 22','BOL 45',...
20        'MOL 45','EOL 45','Location','NorthWest')
21 ylabel('-Im(Z)')
22 xlabel('Re(Z)')

```



# Batixt in Canada – Business Sweden – Supporting JAS 39 Gripen Export



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Thank you for your attention!

–Questions?  
–Discussion.

## References

- Matteo Galeotti, Lucio Cinà, Corrado Giammanco, Stefano Cordiner, and Aldo Di Carlo. Performance analysis and soh (state of health) evaluation of lithium polymer batteries through electrochemical impedance spectroscopy. *Energy*, 89:678–686, 2015. ISSN 0360-5442. doi: <https://doi.org/10.1016/j.energy.2015.05.148>. URL <https://www.sciencedirect.com/science/article/pii/S0360544215007756>.
- Xueyuan Wang, Xuezhe Wei, Jiangong Zhu, Haifeng Dai, Yuejiu Zheng, Xiaoming Xu, and Qijun Chen. A review of modeling, acquisition, and application of lithium-ion battery impedance for onboard battery management. *eTransportation*, 7:100093, 2021. ISSN 2590-1168. doi: <https://doi.org/10.1016/j.etrans.2020.100093>. URL <https://www.sciencedirect.com/science/article/pii/S2590116820300515>.
- Uwe Westerhoff, Kerstin Kurbach, Frank Lienesch, and Michael Kurrat. Analysis of lithium-ion battery models based on electrochemical impedance spectroscopy. *Energy Technology*, 4(12):1620–1630, 2016. ISSN 2194-4296. doi: [10.1002/ente.201600154](https://doi.org/10.1002/ente.201600154). URL <http://dx.doi.org/10.1002/ente.201600154>.

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